



Please solve the following exercises and submit **BEFORE 11:55 p.m. of Friday 18 September.**

**Exercise 1** **(10 points)**

---

Which of these are propositions? What are the truth values of those that are propositions?

- a) The north pole is hot
- b) When is the closest holiday?
- c)  $z^2 > -1$ , for all  $z \in \mathbb{C}$
- d) Do not pass! Just go!
- e) In CMPS 211, there is no raise

**Exercise 2** **(10 points)**

---

Let  $f$ ,  $e$ , and  $h$  be the propositions

- $f$ : You eat healthy food
- $e$ : You exercise regularly
- $h$ : You are in good health

Write these propositions using  $f$ ,  $e$ , and  $h$  and logical connectives (including negations).

- a) If you aren't in good health, then you either don't eat healthy food, or you don't exercise regularly.
- b) You neither eat healthy food, nor you exercise regularly, and you aren't in good health
- c) To exercise regularly, it is necessary that you eat healthy food
- d) Exercising regularly is sufficient for being in good health.
- e) If you aren't in good health, then you don't eat healthy food, and if you don't eat healthy food, then you can't exercise regularly.

**Exercise 3** **(10 points)**

---

Determine whether these bi-conditionals are true or false.

- f)  $-\infty > +\infty$  if and only if  $\frac{0}{0}$  is defined
- g)  $5*5=25$  if and only if  $1-1=2$ .
- h)  $(p \vee \neg p) \leftrightarrow$  Bananas are yellow

**Exercise 4****(10 points)**

Let p and q be the propositions

- d: I do my assignments on my own
- p: I pass my courses

Express each of these propositions as an English sentence.

- a)  $p \rightarrow d$
- b)  $\neg d \wedge \neg p$
- c)  $\neg d \vee (d \wedge p)$

**Exercise 5****(10 points)**

For each of these sentences, determine whether an inclusive or, or an exclusive or, is intended. Explain your answer.

- a) To enter the country you need a passport or a voter registration card.
- b) You can pick Section 1 or Section 2
- c) You either own a Samsung or an iPhone
- d) You either get a full grade or you have some mistake

**Exercise 6****(10 points)**

State the converse, contrapositive, and inverse of each of these conditional statements.

- a) If you solve it fast, then it's wrong
- b) To stay healthy, it's sufficient to drink milk
- c) When I wake up late, it is necessary that I have a full day headache

**Exercise 7****(10 points)**

Construct a truth table for each of these compound propositions.

- a)  $\neg p \rightarrow \neg q$
- b)  $p \leftrightarrow (\neg p \wedge q)$
- c)  $(\neg p \vee \neg q) \rightarrow p$
- d)  $(\neg p \rightarrow \neg q) \leftrightarrow (q \rightarrow p)$
- e)  $(p \leftrightarrow q) \text{ XOR } (p \leftrightarrow \neg q)$

## Exercise 8

(10 points)

What is the value of  $x$  after each of these statements is encountered in a computer program, if  $x = -1$  before the statement is reached?

- if  $x - 3 < 0$  then  $x := (x+1)/2 + 1$
- if  $(2x + 2 = 3)$  OR  $(3x + 1 = 3)$  then  $x := x*2$
- if  $(x + 3 = 2)$  AND  $(3x + 4 = -1)$  then  $x := x-2$
- if  $(x > x)$  XOR  $(x < x)$  then  $x := x+2$
- if  $x < 2$  then  $x := x \bmod 2$  –mod is the modulus function

## Exercise 9

(20 points)

Fuzzy logic is used in artificial intelligence. In fuzzy logic, a proposition has a truth value that is a number between 0 and 1, inclusive. A proposition with a truth value of 0 is false and one with a truth value of 1 is true. Truth values that are between 0 and 1 indicate varying degrees of truth.

For instance, the truth value 0.3 can be assigned to the statement “Tarek is *sick*” because Tarek is *sick* slightly less than half the time, and the truth value 0.9 can be assigned to the statement “Reem is *hungry*” because Reem is *hungry* most of the time. **Use these truth values to solve the following exercises.**

- The truth value of the negation of a proposition in fuzzy logic is 1 minus the truth value of the proposition. What are the truth values of the statements “Tarek is not *sick*”, and “Reem is not *hungry*?”
- The truth value of the conjunction of two propositions in fuzzy logic is the minimum of the truth values of the two propositions. What are the truth values of the statements “Tarek is *sick* and Reem is *hungry*” and “Tarek is not *sick* but Reem is *hungry*?”
- The truth value of the disjunction of two propositions in fuzzy logic is the maximum of the truth values of the two propositions. What are the truth values of the statements “Tarek is *sick*, or Reem is not *hungry*” and “Tarek is not *sick*, or Reem is not *hungry*?”